

Quiz 2

Thursday, July 21. Duration: 50 minutes

1. (*4 points*) Use the method of proof by contradiction to prove the following statement:  
“For all real numbers  $x$ , if  $x^2$  is irrational then  $x$  is irrational.”

2. (*4 points*) Use the Euclidean Algorithm to compute  $\gcd(181, 123)$ . Find integers  $x$  and  $y$  such that  $\gcd(181, 123) = 181x + 123y$ .

Name: \_\_\_\_\_ Id #: \_\_\_\_\_

**3.** (7 points)

Use mathematical induction to prove that  $5^n - 4n - 1$  is divisible by 16 for all integers  $n \geq 1$ .